



**Janet and Mark L.  
Goldenson Center for  
Actuarial Research**

Illuminating Industry Innovation

**DYNAMIC RETIREMENT  
FINANCIAL PLANNING  
MODEL – NOVEMBER 19  
2019 ACHS MEETING  
JAY VADIVELOO & JUSTIN XU**

## Background

- Research work on this topic has generated two PhD theses in actuarial science – Justin Xu and Qintian Sun
- Demonstrates strategic use of Artificial Intelligence and Data Analytics techniques in actuarial science
- Research work is currently being applied to assist a major Goldenson Center client in developing a commercial retirement financial planning model



# Features of an Ideal Retirement Financial Planning Model

- Actuarially sound and easy to understand
- Completely automated
- Incorporates both insurance and investment strategies
- Model captures both volatility in investment returns and changes in health status
- Has a built-in automated recalibration algorithm that adjusts spending patterns annually
- Eliminates ruin probability

# The Risk for Retirees

- No second chances
  - Spending too much and running out of money when they are still alive
  - Spending too little and not experiencing a quality retirement lifestyle
- Failure to plan for differences in spending patterns depending of state of health of retiree



# Current Retirement Financial Planning Models

- Maximize annual spending under an investment strategy
- Insurance products generally not incorporated in the optimal solution
- Does not incorporate changes in spending patterns due to changes in health status
- Generally not an automated process
- No automated recalibration process that adjusts future spending patterns dynamically to eliminate the ruin probability



# Goldenson Center Dynamic Retirement Financial Planning model

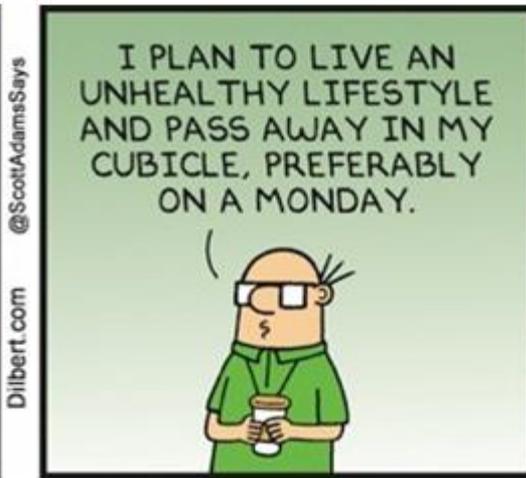
- Has all the features of an ideal retirement planning model
- Models built in R and more recently in Julia to generate solutions in real time (seconds versus hours)
- Uses the MC-MC technique to project future investment returns and health status of retiree
- Uses the AI Kalman Filter technique for annual recalibration of spending and eliminating ruin
- Annual recalibration dynamically connects financial planning with management of retirement assets.
- Maximizes discretionary expenses while ensuring basic expenses are met when the retiree is healthy and unhealthy



Janet and Mark L.  
Goldenson Center for  
Actuarial Research

Illuminating Industry Innovation

# Current Retirement Planning Crisis



Dilbert.com @ScottAdamsSays

© 2016 Scott Adams, Inc. /Dist. by Universal Uclick



# Current Retirement Planning Crisis

- Millions entering retirement every year without a plan
- Goldenson Center model can answer two simple questions:
  - **How much can I spend** in retirement after taxes and inflation?
  - **Will I run out of money** before I run out of breath?



**Janet and Mark L.  
Goldenson Center for  
Actuarial Research**  
Illuminating Industry Innovation

***“[Retirement Income Planning] is a really hard  
problem. It’s the hardest problem I’ve ever looked at.”***

*– William Sharpe*

Nobel Laureate in Economics





# **Key features of Goldenson Center Dynamic Retirement Financial Planning Model:**

# Incorporate Insurance Products-MYGA's

## ➤ Multi-Year Guaranteed Annuities (MYGA)

- Defined as Fixed Rate or CD-type Annuities, is a type of fixed annuity that provide a pre-determined and contractually guaranteed interest rate for a specified period of time

## ➤ Illustrative Examples

- Assume initial assets of \$1M
- 5-year MYGA at the beginning of retirement, fixed rate = 4%
- Asset Market: conservative, moderate, aggressive
- 5% ruin probability

## Results of Financial Planning Example

Asset	MYGA	Opt Allocation	Opt Annual Withdraw
$\mu=2\%$ , $\sigma=2\%$	None	0%	\$39,857
	5 Year, $r=4\%$	77%	\$44,090
$\mu=3\%$ , $\sigma=5\%$	None	0%	\$38,905
	5 Year, $r=4\%$	75%	\$43,195
$\mu=10\%$ , $\sigma=15\%$	None	0%	\$50,449
	5 Year, $r=4\%$	41%	\$54,925

## Comments on Examples

- Incorporating MYGA's to financial planning:
  - Increases annual spending by \$4.5K for each market scenario
  - Neutralizes high volatility in aggressive investment
- Optimal allocation of MYGA decreases with increasing asset return



## **Incorporate Insurance Products—SPIA’s and DIA’s**

- Use SPIA’s to cover basic expenses while healthy
- Use DIA’s to cover increase in basic expenses while unhealthy

## Incorporate HLE

- Defined as the expected future lifetime that one stays healthy
- Termination from a healthy state occurs by death or disability
- Disability uses a long term care definition which is inability to perform some of the activities of daily living
- The only recovery from disability is death
- In contrast, Unhealthy Life Expectancy (ULE) is the expected future lifetime that one stays unhealthy
- $HLE + ULE = \text{Life Expectancy (LE)}$

# Financial Planning Illustrative Example

- Assume initial assets of \$1.5M,  $i = 6\%$ , HLE = 22 years and ULE = 8 years
- Assume PV of basic expenses = 20% of initial assets and covered by a SPIA
- Assume basic expenses are double over ULE period and there are no discretionary expenses, with increased basic expenses covered by a DIA

## Results of Financial Planning Example

- Financial planning not based on HLE:
  - Annual spending over LE of 30 years approximately \$103,000
- Financial planning model based on HLE:
  - Annual spending over HLE approximately \$112,000
  - Annual spending over ULE approximately \$41,000
- Additional annual discretionary spending is \$9,000 or approximately \$750 of additional monthly spending

# Incorporate Kalman-Filter Re-calibration

- Defined as an algorithm that uses the actual performance of daily market return from previous year as sample data to estimate the real  $\mu$  and  $\sigma$
- Combines the result with our prediction at the beginning of previous year based on credibility principles

# Kalman Filter Theory

- Assumes investment returns follow a Brownian Motion process with parameters  $\mu$  and  $\sigma$  estimated from historical returns
- Prior year's annual returns optimally combined with historical returns to recalibrate  $\mu$  and  $\sigma$  parameters
- Adjusts our prediction of optimal retirement spending for the coming year using previous year's optimal spending and revised  $\mu$  and  $\sigma$  parameters

# Incorporate Kalman-Filter Re-calibration

## ➤ Illustrative Example

- Assume  $\mu = 4\%$  and  $\sigma = 10\%$  at beginning of retirement
- Future market either goes up to  $\mu_1 = 8\%$  and  $\sigma = 10\%$ , or goes down to  $\mu_2 = 1.5\%$  and  $\sigma = 10\%$
- Initial asset is \$1M
- Duration is 30 years
- Choose the median path from 1000 simulations as the “actual” path given by  $\mu_1$  and  $\mu_2$
- Comparison between 5%-ruin simple method and Kalman-Filter Re-calibration method

## Results of Financial Planning Example

	Simple	Kalman-Filter
Ending account value ( $\mu_1$ )	\$5,669,360	\$61,074
Average opt withdrawals( $\mu_1$ )	\$32,051	\$100,713
Ruin Probability	0%	0%

- \$5.6M left in the account under simple method
- With Kalman-Filter average annual spending is three times that of the simple method
- No ruin for both methods

## Results of Financial Planning Example

	Sample	Kalman-Filter
Ending account value ( $\mu_2$ )	\$128,272	\$15,221
Average opt withdrawals ( $\mu_2$ )	\$32,051	\$36,273
Ruin Probability	26.4%	0%

- Even under a bad market, Kalman-Filter can still make retiree spend \$4000 more per year on average without ruin
- 26.4% ruin probability means that if retiree chooses to stay with \$32,051 annual spending, it will be highly likely for the retiree to run out of money before he dies

## Comments on Examples

- Eliminates any ruin during retirement under different market performance
- The entire algorithm is fully automated
- Increases average annual spending and also spends retirement assets more efficiently

## Next Steps

- Market dynamic retirement financial planning model to major insurers and financial planning institutions
- Develop a methodology to replace Target Date Funds with more efficient portfolios using a customized combination of investments and annuities
  - The Goldenson Center's TDF algorithm will be dynamically managed and automated to adjust to changes in investment performance and individual health status
  - Will provide both pre and post retirement optimal investment planning



**Janet and Mark L.  
Goldenson Center for  
Actuarial Research**

Illuminating Industry Innovation

*Thank you!*